Study Guide



			2		
II. Function Transformations		E2. $g(x) = -$	$(x-4)^3 - 1$	1. $g(x) = 2^{x-3} + 5$	
General form: $q(x) = a f(x - h) + k$		Parent Function	on:	Parent Function:	
		cubic			
f(x)	parent function	Transformatio	ns:	Transformations:	
$\sigma(\mathbf{x})$	transformed function	flip vertically			
5(^)		shift right 4 un	its		
-	if pagative, flip vortically	shift down 1 u	nit		
а	ii negative, iiip verticaliy				
	0 < a < 1 vertical compression	E3. $g(x) = 3^{-1}$	$\sqrt{x} + 1 - 7$	2 () (π^2	
	<pre> a > 1 vertical stretch</pre>	Parent Functio	on:	2. $g(x) = -(x + 7)^2$	
		Radical (square	e root)	Parent Function:	
h	if negative, horizontal shift right	Transformatio	ns:		
	if positive, horizontal shift left	Stretch by a fa	ctor of 3	Transformations:	
		Shift left 1 unit	Ī		
k	if pagative vertical shift down	Shift down 7 u	nits		
ĸ	if negative, vertical shift wa		into		
	if positive, vertical shift up		1		
		$E4. g(x) = -\frac{1}{2}$	$\frac{1}{2}(x-3)^2+1$	$2 \sigma(u) = 2 \log(u - 2) = 1$	
Exam	ples	Demonst From et la	2	3. $g(x) = 2 \log(x - 2) - 1$	
			n:	Parent Function:	
E1. a	$(x) = x^2 + 2$	quadratic			
Parent	t Function:	Transformatio	ns:	Transformations:	
quadr		Flip vertically			
Transformational		Compression b	by a factor of $\frac{1}{2}$		
chift u	n 2 unite	Shift Dight 2 ur	2 Dite		
shiit u	p z units		iits		
		Shift up 1 unit			
III.Gra	aphing a function from an equation	on - Example	Graph $f(x) = 2$	$2(x-1)^3 - 4$	
1. Ider	htify the parent function to determine a ۽	general shape.		101	
<u>Cubic</u>				8	
				6	
2. Thir	hk about where the vertex or critical poin	ts are usually			
found	for the parent function				
Contor	red at the origin. Is always increasing fro	m laft to right			
Center	ed at the origin. Is always increasing fro		-10 -8 -6 -4 -2	2 4 6 8 10	
o				-2-	
3. Wh	ere are the critical points of the new fund	ction given the		-4	
transf	transformations in the equation? Since there is a horizontal				
<u>shift right 1 unit and a vertical shift down four units, the</u>					
center is at the point (1,-4).				10	
			x y 5.	. Plot the points and connect	
4. Use this information to plan which points to plot on the			, -1 -20 tł	ne dots.	
granh	Make a t table with these points				
Since the center of the aranh is $(1 - 4)$ nick two v values on					
either side of this point and evaluate the $f(x)$ at those x'		those v's			
$\frac{1}{1}$		LIIUSE X S.	2 -2		
			3 12		

Graphing a function from an equa	Graph $f(x) = -(x+3)^3 + 6$		
1. Identify the parent function to determi	ne a general shape.		
2. Think about where the vertex or critica found for the parent function.	l points are usually		
3. Where are the critical points of the new transformations in the equation?	-10 -8 -9 -4 -2 - 2 4 5 6 10 -2 - -4 - -6 -		
4. Use this information to plan which poi	nts to plot on the		
graph. Make a t table with these points.	graph. Make a t table with these points.		
		the dots.	
Writing Function Equation from a	Write the equation	for an absolute value function that has been	
description of the transformations	compressed by a factor of 2 and shifted down three units		
How do translations effect equation?			
f(x) = -a(x - h) + k "-" flip over x axis a compression or stretch h horizontal shift in the opposite direction of the sign k vertical shift in the same direction of the sign	Write the equation shifted up 5 units, a	for a cubic that has been flipped vertically, nd shifted right 2 units.	
EXAMPLE Write the equation for a quadratic function with a vertical shift down 3, left 7 and a vertical stretch by a factor of 4.			
Quadratic : x^2 Down 3: -3 from the function (outside) Left 7: add 7 to x (inside) V. stretch by 4: multiply by 4 $y = 4(x + 7)^2 - 3$			

Determining Equation from Graph What's the parent function?	Example: Write the equation for the following graph.	Write the equation for the following graph	
Where's the vertex or critical point of the parent function?	· /		
Where's the vertex or critical point of this function?	2 (2, 1)	×	
How did we get from the parent function critical point to the critical point of this function?	- ((1, 0)		
How do I translate those changes into an equation?	Cubic so x^3 vertex is up 2, right 1 $y = (x - 1)^3 + 2$		
Shifts of Shifts Apply the stated changes to the appropriate parts of the "starting function".	Example: If the function $f(x) = (x + 1)^2 - 1$, what would be the equation of g(x) if g(x) is f(x) shifted left 3 units, up 2 units, flipped vertically and stretched by a factor of 4?	$f(x) = 2(x)^3 + 4$ Find g(x) if g(x) is f(x) shifted up 2, right 1 and compressed by a factor of 6.	
	Left 3: +3 to x Up 2: +2 Flipped vertically: - in front Stretched by 4: multiplied by 4 $g(x) = -4(x + 1 + 3)^2 - 1 + 2$ $g(x) = -4(x + 4)^2 + 1$	f(x) = - x - 5 Find g(x) if g(x) is f(x) shifted up 4, left 3, stretched by a factor of 2, and flipped vertically.	
Shifts of Shifts part 2 State the transformations to f(x) that would yield g(x)	f(x) = x + 2 - 3 g(x) = -2 x + 1 + 2	$f(x) = -3(x-1)^2 - 3$ $g(x) = -(x+4)^2 - 5$	
Example: $f(x) = -3\sqrt{x-4} + 1$ $g(x) = \frac{3}{5}\sqrt{x+4} + 7$ Was +1, now is +7 so went up 6 Was -4 now is +4 so went left 8 Was 3 now 3/5 so compressed by a factor of 5 Was negative, now positive so flipped vertically			

Study Guide

Real World Functions	Mr. Mealey jumps to dunk a	A crazy engineer is designing an
Use word problems to create and	basketball. The path followed by his	auditorium to have x sections with x+4
analyze a function. Decide what	feet forms a parabola following the	chairs per row and -x+12 chairs per
information is pertinent, and use it to	function $f(t) = -16t^2 + 16t$ where t	column.
answer the questions.	and $f(t)$ is the height of his feet	
E constru	and I(t) is the neight of his feet.	Write an equation for the total
Example:	a. What are the realistic domain and	number of chairs in the auditorium
fact greater than the ennesite of its	range for this graph?	
length		Find a realistic domain
Create an equation to represent the	b. What is the maximum height of his	
area of the sandbox.	feet?	
$A=LW \to A = x(-x+7)$	c. At what time do his feet reach that	Find a realistic range
Find a realistic domain	height?	-
(0,7)many ans. with explanation	6	
Find a realistic range	d. What are his intervals of increase	Find the maximum number of chairs.
(0,12.25) many ans. with exp.	and decrease?	
What is the maximum area?		
12.25 square feet	e. What are his x and y intercepts?	How many sections would create that
What length would create that area?	Why?	number of chairs?
3.5 IEEL		