

## Quadratics - Comparison of Factoring Methods

This document illustrates two methods of factoring quadratic expressions. You may be familiar with the AC method. The SWING method is an alternative method that you may find easier to use.

Notice that Steps 1 through 3 are identical for both methods. Also note that you must put your quadratic expression in standard form before starting this process to insure you assign the correct values to  $a$ ,  $b$ , and  $c$ .

AC	SWING																														
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Another example.

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