Identify the following:
Intervals
Increasing: $(-\infty,-1),(1, \infty)$ Decreasing: $(-1,1)$

X Intercepts: $(-2,0),(0.5,0),(1.5,0)$
Y Intercepts: (0,1)

Relative Maximum(s): ( $-1,3$ )
Relative Minimum(s): ( $1,-1$ )
Domain: $\quad(-\infty, \infty)$
Range: $\quad(-\infty, \infty)$
End Behavior: as $x \rightarrow \infty, y \rightarrow \infty$ as $x \rightarrow-\infty, y \rightarrow-\infty$

## Wednesday, January 28, 2015




| Most confusing Function Characteristics |  |
| :--- | :--- |
| Domain | Interval of X values |
| Range | Interval of Y values |
| Increasing Interval | Interval of X values |
| Decreasing Interval | Interval of X values |
| End Behavior | Look at the far ends of the <br> graph. |
|  | If it's pointing up, Y is <br> approaching positive <br> infinity. |
|  | If it's pointing down, Y is <br> approaching negative <br> infinity. |

## Objectives for today

Review 6 basic parent functions and be able to identify each function from an equation or a graph.

Identify vertical and horizontal function transformations from both a graph and a function equation.
Homework
Complete your parent functions worksheet
Translations on Parent Functions Review even
Any questions from last night's homework?

## Introducing PARENT FUNCTIONS!

Parent functions are the simplest form of families of functions.

| Function | ParentFunction |
| :---: | :---: |
| $g(x)=2 x^{2}+4$ | $f(x)=x^{2}$ |
| $g(x)=x-7$ | $f(x)=x$ |
| $g(x)=\frac{1}{3}(x-7)^{3}-1$ | $f(x)=x^{3}$ |
| $g(x)=\|x+4\|$ | $f(x)=\|\mathrm{x}\|$ |

Constant, $f(x)=C$


Domain:

Range:
End Behavior:

Critical Points:

Increasing/Decreasing:

Linear, $f(x)=x$


Domain:

Range:
End Behavior:
Critical Points:

Increasing/Decreasing:

Quadratic, $f(x)=x^{2}$


Domain:

Range:
End Behavior:
Critical Points:
Increasing/Decreasing:

Square Root
$f(x)=\sqrt{x}$


Domain:

Range:
End Behavior:

Critical Points:

Increasing/Decreasing:

## Cubic

$f(x)=x^{3}$


Domain:

Range:
End Behavior:

Critical Points:

Increasing/Decreasing:

Absolute Value $\boldsymbol{f}(\boldsymbol{x})=|\boldsymbol{x}|$


Domain:

Range:

End Behavior:

Critical Points:
Increasing/Decreasing:

When a function is shifted in any way from its parent function, it is said to be transformed. We call this a transformation of a function. Functions are typically transformed either vertically or horizontally.


## Two categories of Function Transformations

1. Rigid Transformations

The basic shape of the graph is unchanged.
Vertical Shifts
Horizontal Shifts


Reflections

## 2. NonRigid Transformations

Cause a distortion, a change in the graph.
Stretches
Shrinks (Compressions)

Some simple transformations...


Parent Function
Quadratic $f(x)=x^{2}$


Transformed Function
Shifted
Left 3 units
Up 2 units


Transformed Function
Shifted
Right 2 units
Down 2 units

Identify the parent function and the transformations represented in the graphs.



Transformed Function
Shifted
Down 1 unit


Transformed Function
Shifted
Right 2 units
Up 3 units

So how do we represent these transformations algebraically?


Today we will focus on Rigid Transformations

## Vertical Transformations

When functions are transformed on the outside of the $f(x)$ part, you move the function up and down.

| Function Notation | Description of Transformation |
| :---: | :---: |
| $\mathrm{g}(x)=f(x) \pm c$ | Vertical shift up C units if C is positive |
|  | Vertical shift down C units if C is negative |

How do we interpret this function notation?

$$
\begin{aligned}
& \text { Let } f(x)=x^{2} \text { and } c=3 \text { then } g(x)=x^{2}+3 \\
& \text { Let } f(x)=\sqrt{x} \text { and } c=-4 \text { then } g(x)=\sqrt{x}-4 \\
& \text { Let } f(x)=2^{x} \text { and } c=7 \text { then } g(x)=2^{x}+7
\end{aligned}
$$

Let's play "What's going to happen to the parent function?"

| $\boldsymbol{g}(\boldsymbol{x})$ |  |  |
| :---: | :---: | :---: |
| $\boldsymbol{x}$ | $\boldsymbol{x}^{\mathbf{2}}+\mathbf{3}$ |  |
| $\mathbf{X}$ | $\mathrm{f}(\mathrm{x})$ | $\mathrm{g}(\mathrm{x})$ |
|  | $\mathrm{X}^{2}$ | $\mathrm{X}^{2}+3$ |
| 3 | 9 | 12 |
| 2 | 4 | 7 |
| 1 | 1 | 4 |
| 0 | 0 | 3 |
| -1 | 1 | 4 |
| -2 | 4 | 7 |
| -3 | 9 | 12 |



Let's play "What's going to happen to the parent function?"

$$
g(x)=x^{3}-1
$$

| $X$ | $f(x)$ | $g(X)$ |
| :---: | :---: | :---: |
| 3 | $X^{3}$ | $X^{3}-1$ |
| 2 | 8 | 26 |
| 1 | 1 | 0 |
| 0 | 0 | -1 |
| -1 | -1 | -2 |
| -2 | -8 | -9 |
| -3 | -27 | -28 |



Write the equation for the transformed function represented in this graph.

Parent Function? Quadratic, $f(x)=x^{2}$
Critical point that can help us? Vertex
Parent Function? Quadratic, $\boldsymbol{f}(\boldsymbol{x})=$
Critical point that can help us? Vertex

Which way did it go?
Down

By how much?
1 unit

$$
g(x)=x^{2}-1
$$



Write the equation for the transformed function represented in this graph.

Parent Function? Radical, $\boldsymbol{f}(\boldsymbol{x})=\sqrt{\boldsymbol{x}}$
Critical point that can help us? Intercepts

Which way did it go? Up
By how much?
2 units

$$
g(x)=\sqrt{x}+2
$$



## Horizontal Translations

When functions are transformed on the inside of the " $\mathrm{f}(\mathrm{x})$ part", you move the function left and right. Notice the direction is the opposite of the sign inside the " $f(x)$ part".

## Function Notation

$$
g(x)=f(x \pm c)
$$

Description of Transformation
Horizontal shift left $C$ units if $C$ is positive.
Horizontal shift right $C$ units if $C$ is negative

How do we interpret this function notation?

$$
\begin{aligned}
& \text { Let } f(x)=x^{2} \text { and } c=3 \text { then } g(x)=(x+3)^{2} \\
& \text { Let } f(x)=\sqrt{x} \text { and } c=-4 \text { then } g(x)=\sqrt{x-4} \\
& \text { Let } f(x)=2^{x} \text { and } c=7 \text { then } g(x)=2^{x+7}
\end{aligned}
$$

Let's play "What's going to happen to the parent function?"

$$
g(x)=(x-1)^{2}
$$



Let's play "What's going to happen to the parent function?"

$$
g(x)=(x+2)^{3}
$$



## Write the equation for the transformed function represented in this graph.

Parent Function?
Cubic, $f(x)=x^{3}$
Critical point that can help us? Intercepts
Which way did it go?
Left

By how much?
1 unit

$$
g(x)=(x-1)^{3}
$$



Write the equation for

$$
f(x)=(x-2)^{3}+1
$$

the transformed function represented in this graph.

Parent Function?<br>Cubic, $f(x)=x^{3}$<br>Critical point that can help us? Intercepts<br>Which way did it go?<br>By how much?<br>Left and up<br>Left 2 and up 1



## Reflections

When a negative sign is found on the outside of the " $f(x)$ part" the function is flipped over the $\mathbf{x}$-axis.

## Function Notation <br> Description of Transformation

$g(x)=-f(x)$
Reflected over the $x$-axis

How do we interpret this function notation?

$$
\begin{aligned}
& \text { Let } f(x)=x^{2} \text {, then }-f(x)=-x^{2} \\
& \text { Let } f(x)=\sqrt{x}, \text { then }-f(x)=-\sqrt{x}
\end{aligned}
$$

Flip across the x axis

| $\boldsymbol{f}(\boldsymbol{x})=-\boldsymbol{x}^{\mathbf{2}}$ |  |  |
| :---: | :---: | :---: |
| X | $\mathrm{X}^{2}$ | $-\mathrm{X}^{2}$ |
| 3 | 9 | -9 |
| 2 | 4 | -4 |
| 1 | 1 | -1 |
| 0 | 0 | 0 |
| -1 | 1 | -1 |
| -2 | 4 | -4 |
| -3 | 9 | -9 |



Flip across the $y$ axis

| $\boldsymbol{f}(\boldsymbol{x})=(-\boldsymbol{x})^{\mathbf{3}}$ |  |  |
| :---: | :---: | :---: |
| $\mathbf{X}$ | $-\mathbf{X}$ | $(-\mathrm{X})^{3}$ |
| 3 | -3 | -27 |
| 2 | -2 | -8 |
| 1 | -1 | -1 |
| 0 | 0 | 0 |
| -1 | 1 | 1 |
| -2 | 2 | 8 |
| -3 | 3 | 27 |



## Write the equation for the transformed function represented in this graph.

Parent Function? Radical, $\boldsymbol{f}(\boldsymbol{x})=\sqrt{\boldsymbol{x}}$
Critical point that can help us? Intercepts
Which way did it go? No Change
Which axis has it flipped over? X-axis

$$
f(x)=-\sqrt{x}
$$



## Summary of the Rigid Transformations

| Function Notation | Description of Transformation |
| :---: | :---: |
| $\mathrm{g}(x)=f(x) \pm c$ | Vertical shift up C units if C is positive |
|  | Vertical shift down C units if C is negative |


| Function Notation | Description of Transformation |
| :---: | :---: |
| $g(x)=f(x \pm c)$ | Horizontal shift left C units if C is positive. |
|  | Horizontal shift right C units if C is negative |
| Function Notation | Description of Transformation |
| $\mathrm{g}(x)=-f(x)$ | Flipped over the x -axis |

Did we meet our objectives?


