## Sunday, February 1, 2015

Draw a graph with the following characteristics:
Maximums at $(-3,4)$ and $(2,2)$
Minimum at (-1,-3)
$X$ intercepts at $(-4,0),(-2,0),(1,0)$, and $(3,0)$
Y intercept at ( $0,-2$ )
Increasing Intervals $(-\infty,-3)$ and $(-1,2)$
Decreasing Intervals ( $-3 .-1$ ) and ( $2, \infty$ )


HINT: plot points first then connect the dots.

## Objectives for today

Review 6 basic parent functions and be able to identify each function from an equation or a graph. Identify the characteristics of Parent Functions.

## Homework

Complete your parent functions worksheet
Complete Domain/Range worksheet

Homework Review
Check your answers.

## Last time we met...

Domain and Range - What do we look at to determine?
Look at x values for Domain and y values for Range
Maximums and Minimums - What do these look like on the graphs?
Maximums are peaks in the graph and Minimums are valleys
$X$ and $Y$ Intercepts - Where are these found on the graph?
Intercepts are where the graph crosses the x and y axis
Increasing/Decreasing Intervals - How do we describe these intervals?
Use interval notation, use the x axis to define you interval

# Look at your packet - Domain and Range worksheet 

In groups or by yourself, work on problems 1-12

We'll work on 13 and 14 together

## Introducing PARENT FUNCTIONS!

Parent functions are the simplest form of families of functions.

| Function | Parent Function |
| :---: | :---: |
| $g(x)=2 x^{2}+4$ | $f(x)=x^{2}$ |
| $g(x)=x-7$ | $f(x)=x$ |
| $g(x)=\frac{1}{3}(x-7)^{3}-1$ | $f(x)=x^{3}$ |
| $g(x)=\|x+4\|$ | $f(x)=\|\mathrm{x}\|$ |



Constant, $f(x)=C$

| Domain | Range |  |  |
| :--- | :---: | :---: | :---: |
| End Behavior |  |  |  |
| as $x \rightarrow-\infty, y \rightarrow$ | as $x \rightarrow \infty, y \rightarrow$ |  |  |
| Critical Points |  |  |  |
| Vertex | X intercepts |  |  |

## Linear, $f(x)=x$



| Domain | Range |  |
| :--- | :---: | :---: |
| End Behavior |  |  |
| as $x \rightarrow-\infty, y \rightarrow$ | as $x \rightarrow \infty, y \rightarrow$ |  |
| Critical Points |  |  |
| Vertex | X intercepts $\quad$ intercepts |  |



## Quadratic, $f(x)=x^{2}$

| Domain | Range |  |
| :--- | :---: | :---: |
|  | End Behavior |  |
| as $x \rightarrow-\infty, y \rightarrow$ | as $x \rightarrow \infty, y \rightarrow$ |  |
| Critical Points |  |  |
| Vertex | X intercepts $\quad$ intercepts |  |



## Radical (Square Root), $f(x)=$

| Domain | Range |  |
| :--- | :---: | :---: |
| End Behavior |  |  |
| as $x \rightarrow-\infty, y \rightarrow$ | as $x \rightarrow \infty, y \rightarrow$ |  |
| Critical Points |  |  |
| Vertex | X intercepts $\quad$ intercepts |  |

Work with a partner to complete the remaining two functions.
Cubic, $f(x)=x^{3}$


Absolute Value, $f(x)=|x|$


| Domain | Range |
| :--- | :---: |
| End Behavior |  |
| as $x \rightarrow-\infty, y \rightarrow$ | as $x \rightarrow \infty, y \rightarrow$ |

## Critical Points

Center $X$ intercepts $\quad Y$ intercepts

| Domain | Range |  |
| :--- | :---: | :---: |
|  | End Behavior |  |
| as $x \rightarrow-\infty, y \rightarrow$ | as $x \rightarrow \infty, y \rightarrow$ |  |
| Critical Points |  |  |
| Vertex | $\mathbf{X}$ intercepts $\quad$ intercepts |  |

When a function is shifted in any way from its parent function, it is said to be transformed. We call this a transformation of a function. Functions are typically transformed either vertically or horizontally.


## Two categories of Function Transformations

1. Rigid Transformations

The basic shape of the graph is unchanged.
Vertical Shifts
Horizontal Shifts
Reflections
2. NonRigid Transformations

Cause a distortion, a change in the graph.
Stretches
Shrinks (Compressions)

## Some simple transformations...



Parent Function
Quadratic $f(x)=x^{2}$


Transformed Function
Shifted
Left 3 units
Up 2 units


Transformed Function
Shifted
Right 2 units
Down 2 units

Identify the parent function and the transformations represented in the graphs.


Parent Function
Cubic
$f(x)=x^{3}$


Transformed Function
Shifted
Down 1 unit


Transformed Function
Shifted Right 2 units Up 3 units

So how do we represent these transformations algebraically?


Today we will focus on Rigid Transformations

## Vertical Transformations

When functions are transformed on the outside of the $f(x)$ part, you move the function up and down.

| Function Notation | Description of Transformation |
| :---: | :---: |
| $\mathrm{g}(x)=f(x) \pm c$ | Vertical shift up C units if C is positive |
|  | Vertical shift down C units if C is negative |

## Vertical Transformations

| Function Notation | Description of Transformation |
| :---: | :---: |
| $\mathrm{g}(x)=f(x) \pm c$ | Vertical shift up C units if C is positive |
|  | Vertical shift down C units if C is negative |

How do we interpret this function notation?

$$
\begin{aligned}
& \text { Let } f(x)=x^{2} \text { and } c=3 \text { then } g(x)=x^{2}+3 \\
& \text { Let } f(x)=\sqrt{x} \text { and } c=-4 \text { then } g(x)=\sqrt{x}-4 \\
& \text { Let } f(x)=2^{x} \text { and } c=7 \text { then } g(x)=2^{x}+7
\end{aligned}
$$

Let's play "What's going to happen to the parent function?"

| $\boldsymbol{g}(\boldsymbol{x})$ |  |  |
| :---: | :---: | :---: |
| $\boldsymbol{y}$ | $\boldsymbol{x}^{\mathbf{2}}+\mathbf{3}$ |  |
| $\mathbf{X}$ | $\mathrm{f}(\mathrm{x})$ | $\mathrm{g}(\mathrm{x})$ |
|  | $\mathrm{X}^{2}$ | $\mathrm{X}^{2}+3$ |
| 3 | 9 | 12 |
| 2 | 4 | 7 |
| 1 | 1 | 4 |
| 0 | 0 | 3 |
| -1 | 1 | 4 |
| -2 | 4 | 7 |
| -3 | 9 | 12 |



Let's play "What's going to happen to the parent function?"

| $\boldsymbol{g}(\boldsymbol{x})=\boldsymbol{x}^{\mathbf{3}}-\mathbf{1}$ |  |  |
| :---: | :---: | :---: |
| X | $\mathrm{f}(\mathrm{x})$ | $\mathrm{g}(\mathrm{x})$ |
|  | $\mathrm{X}^{3}$ | $\mathrm{X}^{3}-1$ |
| 3 | 27 | 26 |
| 2 | 8 | 7 |
| 1 | 1 | 0 |
| 0 | 0 | -1 |
| -1 | -1 | -2 |
| -2 | -8 | -9 |
| -3 | -27 | -28 |



## Write the equation for the transformed function <br> represented in this graph.

Parent Function? Quadratic, $f(x)=x^{2}$

Which way did it go? Down

By how much?
1 unit

$$
g(x)=x^{2}-1
$$

## Critical point that can help us? Vertex

Which way did it go? Dow
By how much? 1 unit


Write the equation for the transformed function represented in this graph.

Parent Function? Log, $\boldsymbol{f}(\boldsymbol{x})=\boldsymbol{b}^{\boldsymbol{x}}$
Critical point that can help us? Intercepts

Which way did it go? Down

By how much? 2 units

$$
g(x)=b^{x}-2
$$



## Write the equation for the transformed function represented in this graph.

Parent Function? Radical, $\boldsymbol{f}(\boldsymbol{x})=\sqrt{\boldsymbol{x}}$
Critical point that can help us? Intercepts
Which way did it go? Up
By how much? 2 units

$$
g(x)=\sqrt{x}+2
$$



## Horizontal Translations

When functions are transformed on the inside of the " $\mathrm{f}(\mathrm{x})$ part", you move the function left and right. Notice the direction is the opposite of the sign inside the " $\mathrm{f}(\mathrm{x})$ part".

| Function Notation | Description of Transformation |
| :---: | :---: |
| $g(x)=f(x \pm c)$ | Horizontal shift left C units if C is positive. |
|  | Horizontal shift right C units if C is negative |

## Horizontal Translations

| Function Notation | Description of Transformation |
| :--- | :--- |
| $g(x)=f(x \pm c)$ | Horizontal shift left C units if C is positive. |
|  | Horizontal shift right C units if C is negative |

How do we interpret this function notation?

$$
\begin{aligned}
& \text { Let } f(x)=x^{2} \text { and } c=3 \text { then } g(x)=(x+3)^{2} \\
& \text { Let } f(x)=\sqrt{x} \text { and } c=-4 \text { then } g(x)=\sqrt{x-4} \\
& \text { Let } f(x)=2^{x} \text { and } c=7 \text { then } g(x)=2^{x+7}
\end{aligned}
$$

Let's play "What's going to happen to the parent function?"

$$
g(x)=(x-1)^{2}
$$



Let's play "What's going to happen to the parent function?"

$$
g(x)=(x+2)^{3}
$$



Write the equation for the transformed function represented in this graph.

Parent Function?

Cubic, $f(x)=x^{3}$
Critical point that can help us? Intercepts
Which way did it go? Left
By how much?
1 unit


Write the equation for the transformed function represented in this graph.

Parent Function? Log, $\boldsymbol{f}(\boldsymbol{x})=\boldsymbol{\operatorname { L o g }} \boldsymbol{x}$
Critical point that can help us? Intercepts
Which way did it go? Right
By how much? 2 units

$$
f(x)=\log (x-2)
$$



Write the equation for the transformed function represented in this graph.
Parent Function?
Cubic, $f(x)=x^{3}$

Critical point that can help us? Intercepts
Which way did it go? Left and up
By how much?
Left 2 and up 1

$$
f(x)=(x-2)^{3}+1
$$



## Reflections

When a negative sign is found on the outside of the " $f(x)$ part" the function is flipped over the $x$-axis.

When a negative sign is found on the inside of the " $f(x)$ part" the function is flipped over the $\mathbf{y}$-axis.

| Function Notation | Description of Transformation |
| :--- | :--- |
| $\mathrm{g}(x)=-f(x)$ | Reflected over the x -axis |
| $\mathrm{g}(x)=f(-x)$ | Reflected over the $y$-axis |

## Reflections

| Function Notation | Description of Transformation |
| :--- | :--- |
| $\mathrm{g}(x)=-f(x)$ | Reflected over the x -axis |
| $\mathrm{g}(x)=f(-x)$ | Reflected over the y -axis |

How do we interpret this function notation?

$$
\begin{aligned}
& \text { Let } f(x)=x^{2} \text {, then }-f(x)=-x^{2} \text { and } f(-x)=(-x)^{2} \\
& \text { Let } f(x)=\sqrt{x} \text {, then }-f(x)=-\sqrt{x} \text { and } f(-x)=\sqrt{-x} \\
& \text { Let } f(x)=2^{x} \text {, then }-f(x)=-2^{x} \text { and } f(-x)=2^{-x}
\end{aligned}
$$

Reflection across the $x$ axis

| $\boldsymbol{f}(\boldsymbol{x})=-\boldsymbol{x}^{\mathbf{2}}$ |  |  |
| :---: | :---: | :---: |
| X | $\mathrm{X}^{2}$ | $-\mathrm{X}^{2}$ |
| 3 | 9 | -9 |
| 2 | 4 | -4 |
| 1 | 1 | -1 |
| 0 | 0 | 0 |
| -1 | 1 | -1 |
| -2 | 4 | -4 |
| -3 | 9 | -9 |



Reflection across the $y$ axis

| $\boldsymbol{f}(\boldsymbol{x})=(-\boldsymbol{x})^{\mathbf{3}}$ |  |  |
| :---: | :---: | :---: |
| $\mathbf{X}$ | $-\mathbf{X}$ | $(-X)^{3}$ |
| 3 | -3 | -27 |
| 2 | -2 | -8 |
| 1 | -1 | -1 |
| 0 | 0 | 0 |
| -1 | 1 | 1 |
| -2 | 2 | 8 |
| -3 | 3 | 27 |



## Write the equation for the transformed function represented in this graph.

Parent Function? Radical, $\boldsymbol{f}(\boldsymbol{x})=\sqrt{\boldsymbol{x}}$
Critical point that can help us? Intercepts
Which way did it go? No Change
Which axis has it flipped over? X-axis

$$
f(x)=-\sqrt{x}
$$



## Summary of the Rigid Transformations

| Function Notation | Description of Transformation |
| :---: | :---: |
| $\mathrm{g}(x)=f(x) \pm c$ | Vertical shift up C units if C is positive |
|  | Vertical shift down $C$ units if $C$ is negative |


| Function Notation | Description of Transformation |
| :---: | :---: |
| $g(x)=f(x \pm c)$ | Horizontal shift left C units if C is positive. |
|  | Horizontal shift right C units if C is negative |
| Function Notation | Description of Transformation |
| $\mathrm{g}(x)=-f(x)$ | Reflected over the x -axis |
| $\mathrm{g}(x)=f(-x)$ | Reflected over the y -axis |

## Did we meet our objectives?



